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Inductive seismo-electromagnetic effect in relation to seismogenic ULF emission

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Abstract. During the seismic wave propagation through the crust, the electromagnetic pulse can originate due to MHD conversion in this conductive medium. On the assumption of simple models of seismic wave excitation and attenuation, the problem is reduced to the analysis of a diffusion-like equation for a vector potential function. In this way, we need to change the classical gauge condition. A semi-analytical form of the solution is obtained in a case with constant ground conductivity. Dependencies of the electric and magnetic field components and the pulse duration on distance and crust conductivity have been computed in detail. The results could be useful for the explanation of electromagnetic signals related to coseismic, foreshock and aftershock activity.

1 Introduction

ULF (ultra-low frequency, $f = 0.003 - 10$ Hz) electromagnetic emissions have been observed prior to the occurrence of earthquakes in the USA, Russia, and Japan (see references in Hayakawa, 1999). It is rather difficult to find theoretical mechanisms of this phenomenon. Fenoglio et al. (1994) proposed a model of ruptured isolated reservoirs, resulting in the electro-kinetic (EK) generation of a transient magnetic field. However, they neglected the compensating conduction current inside the path of the EK current and they oversimplified the problem. Therefore, EK generation can be used for the interpretation of so-called seismo-electric signals (SES), but not for ULF magnetic emission (Molchanov, 1999).

A mechanism of ULF electromagnetic field generation based on the ensemble crack opening (microfracturing) was considered by Molchanov and Hayakawa (1995). Creation and relaxation of charges at the walls of opening cracks in the earthquake hypocenter was proposed as a possible reason for electromagnetic noise prior to the earthquake. The

other approach was suggested by Surkov (1999), Surkov et al. (2000), and Molchanov et al. (2001). Their theory is based on the same assumption of microfracturing, but the electromagnetic perturbation is caused by an MHD (inductive) effect from a propagating seismic wave. An inductive seismo-magnetic effect from a solitary seismic wave was assumed in relation to the observation of so-called magnetic forerunners or coseismic magnetic perturbations (Eleman, 1965; Belov et al., 1974). Recently, the coseismic electric signals were also observed (Takeuchi et al., 1997; Nagao et al., 2000).

The next problem is the penetration of the electromagnetic fields through a dissipative ground medium. The conventional way is to consider static fields. For example, Fenoglio et al. (1994) applied the Biot-Savart law for the estimation of magnetic variations from the opening fracture. But Kawate et al. (1998) found a clear difference between the results of modeling on the suppositions of Biot-Savart law and full-wave procedure. However, they have assumed a quasi-stationary source. The same approach of quasi-stationarity is conventional for magneto-telluric (MT) or telluric calculations (e.g. Ward and Hohmann, 1988), but it is not valid for our case of a pulsing source. In a low-frequency (LF) domain after neglecting the displacement currents (it is valid for a ground medium if $f < 1$ MHz), Maxwell equations can be reduced to the well-known equations of electromagnetic diffusion (e.g. Hohmann, 1988):

$$\frac{1}{D} \frac{\partial \mathbf{H}}{\partial t} - \nabla^2 \mathbf{H} = \nabla \times \mathbf{j}_s + \nabla \sigma \times \mathbf{E}, \quad D = \frac{1}{\mu \sigma}, \quad (1)$$

$$\begin{aligned} \frac{1}{D} \frac{\partial \mathbf{E}}{\partial t} - \nabla^2 \mathbf{E} = & \nabla \left(\frac{1}{\sigma} \nabla \cdot \mathbf{j}_s \right) \\ & + \nabla \left(\mathbf{E} \cdot \frac{\nabla \sigma}{\sigma} \right) - \mu \frac{\partial \mathbf{j}_s}{\partial t} \end{aligned} \quad (2)$$

where \mathbf{E} , \mathbf{H} , \mathbf{j}_s are the vectors of electric and magnetic fields and source current density, σ , μ are conductivity and magnetic permeability, and $D = (\sigma \mu)^{-1}$ is the coefficient of electromagnetic diffusion.

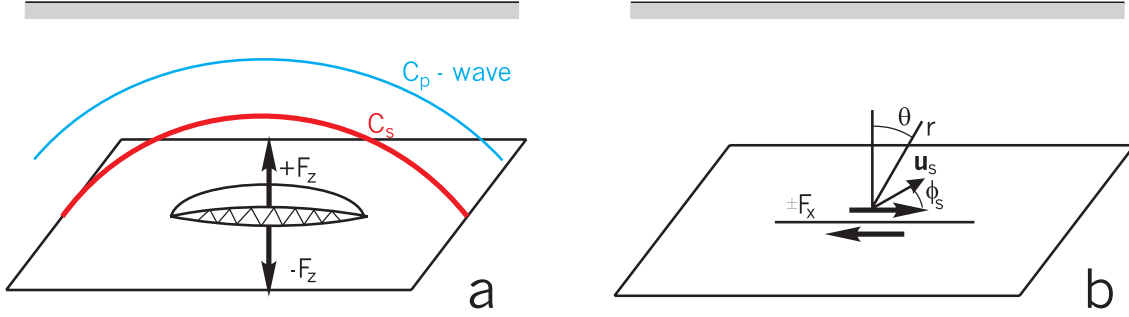


Fig. 1. Scheme of tension (a) shear (b) cracks.

These equations are rather popular in MHD theory and could be used for the special assumptions on parameters (e.g. frozen electric field). But in our case, they lead to great complications due to the imposing vectorial operators on the source current. For example, even by using the assumption of constant conductivity, Surkov et al. (2000) have succeeded in obtaining only asymptotic behaviour of the solutions, which cannot be checked in a static limit and cannot be applied for comparison with observational data. The numerical solution of these equations are sometimes used in an MT study in order to analyze the transient fields (Hohmann, 1988; Pellerin and Hohmann, 1995). But such 4-D computations usually require a lot of time and also cannot be checked in dependence on the task parameters. We found that this is the best way to use the classical double-potential method but with special modification of the gauge condition.

2 Basic equations

Vectorial potential \mathbf{A} and scalar potential φ are introduced in the usual manner:

$$\mathbf{H} = \nabla \times \mathbf{A} \quad \mathbf{E} = -\mu \frac{\partial \mathbf{A}}{\partial t} - \nabla \varphi. \quad (3)$$

These potentials are not completely independent from each other. Their connection is determined by the so-called gauge; its classical (Lorentz) form is the following (Landau and Lifshits, 1992):

$$\nabla \cdot \mathbf{A} + \varepsilon \frac{\partial \varphi}{\partial t} = 0 \quad \text{or} \quad \nabla \cdot \mathbf{A} = 0. \quad (4)$$

The last relationship is conventional in LF and static approximation. But this gauge cannot give separated second order equations for the potentials in the case of $\sigma \neq 0$. On the other hand, it is usual (e.g. in plasma physics) to include the conductivity influence through the effective, complex permittivity coefficient $\varepsilon' = \varepsilon (1 + i\sigma/\omega\varepsilon)$. It identified how the classic gauge could be modified. Remembering that operator $\partial/\partial t \simeq -i\omega$, we can rewrite this gauge as follows:

$$\begin{aligned} \nabla \cdot \mathbf{A} + \varepsilon' \frac{\partial \varphi}{\partial t} &= \nabla \cdot \mathbf{A} + \varepsilon \left(1 + \frac{i\sigma}{\omega\varepsilon} \right) (-i\omega\varphi) \simeq \\ \nabla \cdot \mathbf{A} + \varepsilon \frac{\partial \varphi}{\partial t} + \sigma\varphi &= 0 \end{aligned} \quad (5)$$

and introduce a new gauge for the conductive medium in LF approximation:

$$\nabla \cdot \mathbf{A} + \sigma\varphi = \text{const}. \quad (6)$$

Using this gauge, the equations for vectorial and scalar potentials are written as follows:

$$\frac{1}{D} \frac{\partial \mathbf{A}}{\partial t} - \nabla^2 \mathbf{A} + (\nabla\sigma/\sigma)\nabla \cdot \mathbf{A} = \mathbf{j}_s \quad (7)$$

$$\nabla(\sigma\varphi) = -\nabla(\nabla \cdot \mathbf{A}). \quad (8)$$

Of course, these equations are more convenient for computations than Eqs. (1, 2) and Eq. (7) clearly represents the combination of diffusion and convection processes. But in the case of a homogeneous conductive medium, the situation is reduced to a symmetrical view of simple diffusion equations:

$$\frac{1}{D} \frac{\partial \mathbf{A}}{\partial t} - \nabla^2 \mathbf{A} = \mathbf{j}_s \quad (9)$$

$$\frac{1}{D} \frac{\partial \varphi}{\partial t} - \nabla^2 \varphi = -\nabla \cdot \mathbf{j}_s / \sigma \quad (10)$$

where $D = (\sigma\mu)^{-1}$ is the coefficient of electromagnetic diffusion.

The electric field induced in the conductor moving with velocity \mathbf{v} under the permanent magnetic field \mathbf{H}_0 is known:

$$\mathbf{E}' = \mu \mathbf{v} \times \mathbf{H}_0 \quad (11)$$

assuming $\mathbf{H} \ll \mathbf{H}_0$. In our case, $\mathbf{v} = \partial \mathbf{u} / \partial t$, where \mathbf{u} is a vector of ground displacement produced by a seismic wave, and the resultant source current is given by,

$$\mathbf{j}_s = \sigma \mathbf{E}' = \frac{1}{D} \frac{\partial \mathbf{u}}{\partial t} \times \mathbf{H}_0 \quad (12)$$

3 Model of seismic perturbation

In general, the seismic source is characterized by seismic moment density tensor (Aki and Richards, 1980). However, for the description of far-distance displacement (distance $r \gg L_s$, the last is the source dimension), the seismic moment M , which is proportional to the faulting area $A_s \sim L_s^2$ and slip $[u]$, is conventionally used. It is equivalent

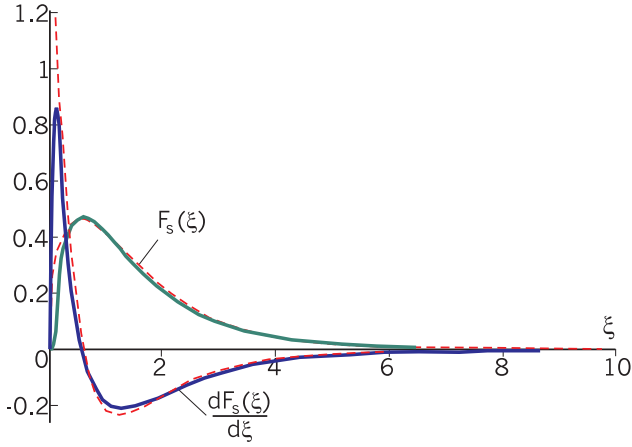


Fig. 2. Function $F_s(\xi)$ and $dF_s/d\xi$ (Eq. (20)). Solid line is the approximation.

to the supposition of the point source and a couple of body forces. There are two limiting cases in such a way (Fig. 1). The first is a case of expansion or tension crack when a force direction (direction of strike) is perpendicular to the faulting plane (Fig. 1a). The second (Fig. 1b) is a case of shear dislocation when strike and slip are in the faulting plane. Two waves are propagating from the seismic source with velocity $C_p = \sqrt{(l + 2m)/\rho}$ (primary wave P) and $C_s = \sqrt{m/\rho}$, where m, l are Lamé's coefficients and ρ is the ground density. By neglecting attenuation, they create the following displacements (Aki and Richards, 1980):

a) in the case of a tension crack, $M_t = l A_s [u_z]$,

$$u_t^i = \frac{a_t^i}{4\pi\rho C_i^3 r} \frac{\partial M_t(t - r/C_i)}{\partial t} \quad (13)$$

where $i = P, S$. In the spherical coordinate system with unity vectors $\mathbf{e}_r, \mathbf{e}_\theta, \mathbf{e}_\phi$ (axis $\theta = 0$ is perpendicular to the faulting plane, and axis $\phi = 0$ is the strike direction), the polarization vectors are the following:

$$\mathbf{a}_t^P = (1 + 2m \cos^2 \theta / l) \mathbf{e}_r, \quad \mathbf{a}_t^S = -m \sin 2\theta \mathbf{e}_\theta / l \quad (14)$$

b) in the case of a shear crack, $M_{sh} = m A_s [u_x]$

$$u_{sh}^i = \frac{a_{sh}^i}{4\pi C_i^3 r} \frac{\partial M_{sh}(t - r/C_i)}{\partial t} \quad (15)$$

and

$$\begin{aligned} \mathbf{a}_{sh}^P &= \sin 2\theta \cos(\phi - \phi_s) \mathbf{e}_r, \\ \mathbf{a}_{sh}^S &= \cos 2\theta \cos(\phi - \phi_s) \mathbf{e}_\theta \\ &= \cos \theta \sin(\phi - \phi_s) \mathbf{e}_\phi \end{aligned} \quad (16)$$

where ϕ_s is the angle between the directions of strike and slip (see Fig. 1b).

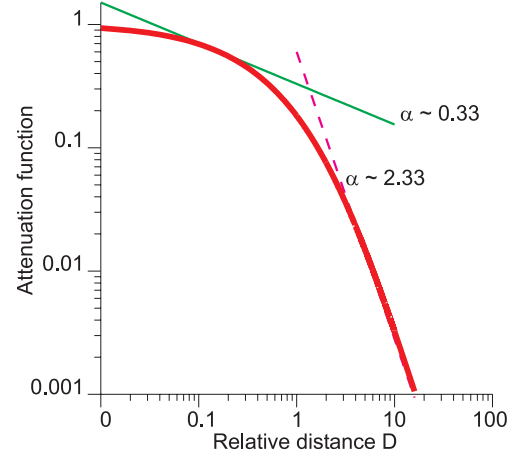


Fig. 3. Attenuation function for the relative distance r/R_a . It can be represented by the dependence $(r/R_a)^{-\alpha}$, where $\alpha \approx 2.33$ for $r \geq 3R_a$ and averaged $\alpha \approx 0.33$ for the values $r \leq R_a$.

Lamé's coefficients are related with rigidity $K_t = 2m$ and the Poisson ratio p : $l = K_t p / (1 - 2p)$. As usual in theory, we assume $p \sim 0.33$, so $l \sim K_t$ and $C_p \sim 2C_s$. Furthermore, we simplify the problem supposing:

- \mathbf{H}_0 is parallel to the axis $\theta = 0$
- $\phi_s = 0$

Eqs. (13, 15) include the dependence of $\partial M / \partial t$ on retard time $t - r/C_i \geq 0$.

The temporal evolution of $M(r, t)$ can be expressed as follows:

$$M|_{t \geq 0} = \int_0^\infty M(\omega/\omega_c) e^{-i\omega t} d\omega \quad (17)$$

where ω_c is a “corner” frequency of the seismic spectrum and $\omega_c \tau = q_0 \approx 2$ (e.g. Brune et al., 1979), $\tau \approx L_s / C_R$ is the duration of the slip, and C_R is the rupture velocity. $M(\omega/\omega_c)$ is proportional to ω^{-3} in the high frequency ($\omega \gg \omega_c$) part of the spectrum (Aki and Richards, 1980, Scholz, 1990). So the convenient representation is the following:

$$M(\omega/\omega_c) = (M_0/\omega_c) / [1 + (\omega/\omega_c)^2]^{3/2} \quad (18)$$

where $M_0 = K_t A_s [u_z^0]$ for a tension crack or $M_0 = K_t A_s [u_x]/2$ for a shear crack. Hence, by neglecting attenuation, we obtain

$$\left. \frac{\partial M}{\partial t} \right|_{t \geq r/C_i} = M_0 \omega_c F_s(\xi) \quad (19)$$

where $\xi = \omega_c(t - r/C_i)$, and for the displacement, we have

$$F_s(\xi) = \int_0^\infty \frac{x \sin(x\xi) dx}{(1+x^2)^{3/2}} \approx 20\pi \xi^2 \exp(-5\sqrt{\xi}) \quad (20)$$

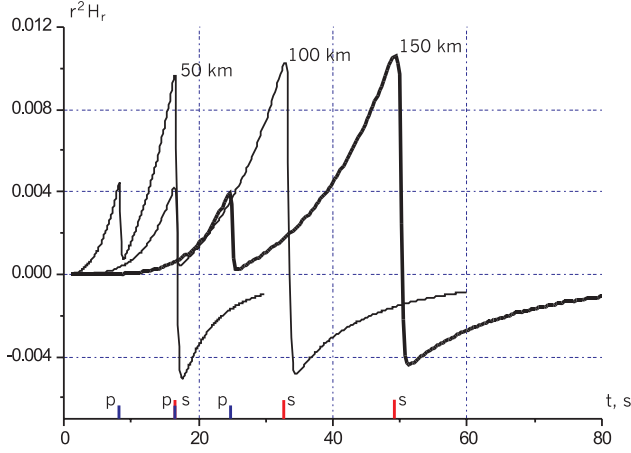


Fig. 4. Calculation $r^2 H_r(t)$ for $r = 50$ km, $r = 100$ km, $r = 150$ km. $\theta = 15^\circ$. Figure shows that $H_r \sim 1/r^2$. Time of primary (p) and secondary (s) seismic wave are highlighted.

The last expression is a useful approximation that is demonstrated in Fig. 2. For this approximation, $dF_s/d\xi$ (velocity) is limited for all $\xi \in [0, +\infty)$. Furthermore, the condition of summary displacement $\int_0^{+\infty} dF_s(\xi) = 0$ is true.

As a result, the induced source currents are the following:

$$\mathbf{j}_t = B_t \{ f^P(r, t) \sin \theta (1 + \cos^2 \theta) + 8 f^S(r, t) \sin \theta \cos^2 \theta \} \mathbf{e}_\phi \quad (21)$$

$$\mathbf{j}_{sh} = B_{sh} \{ f^P \sin \theta \sin 2\theta \cos \phi \mathbf{e}_\phi + 8 f^S \cos \theta [\sin \theta \sin \phi \mathbf{e}_r + \cos \theta \sin \phi \mathbf{e}_\theta + \cos 2\theta \cos \phi \mathbf{e}_\phi] \} \quad (22)$$

where

$$B_t = H_0 A_s C_R [u_z^0] / (8\pi D C_p L_s^2) \approx C H_0 [u_z^0] / (16D)$$

assuming

$$C \approx C_R \approx C_s \approx C_p/2, \quad B_{sh} \approx C H_0 [u_x^0] / (32D)$$

and

$$f^i = (T_a^i/r) \frac{\partial F_s}{\partial \xi}, \quad \xi = 2(t - t_s^i)/\tau \geq 0 \quad (23)$$

$t_s^i = r/C_i$, $i = P, S$. Here, T_a^i is an attenuation function. It depends on the spectrum of seismic pulse (see Molchanov et al., 2001):

$$T_a^i = \left\{ \int \omega^4 M^2(\omega/\omega_c) \exp(-2\omega r/\omega_c R_a^i) d\omega / \int \omega^4 M^2(\omega/\omega_c) d\omega \right\}^{1/2} \quad (24)$$

where $R_a^i = 2QC_i/\omega_c \approx QL_s C_i/C$ is an attenuation distance, Q is a seismic quality ($Q \approx 100$). Assuming (18), we have the following expression for T_a :

$$T_a(r/R_a) = \frac{4}{\sqrt{3\pi}} \left\{ \int_0^\infty x^4 \exp(-2xr/R_a) dx / (1+x^2)^3 \right\}^{1/2} \quad (25)$$

where $R_a^i \approx QL_s C_i/C$. The dependence of $T_a(r/R_a)$ is given in Fig. 3.

4 Solution for a tension crack

In this case, $\mathbf{A} = A \mathbf{e}_\phi$, $\nabla \cdot \mathbf{A} = 0$, $\varphi = 0$, $E_\phi = -\mu \partial A / \partial t$, $H_r = (1/r \sin \theta) \partial(\sin \theta A) / \partial \theta$, $H_\theta = -(1/r) \partial(rA) / \partial r$, $H_\phi = E_r = E_\theta = 0$ and the basic equation (9) is reduced to the following:

$$\frac{1}{D} \frac{\partial A^i}{\partial t} - \frac{1}{r^2} \frac{\partial}{\partial r} \left(r^2 \frac{\partial A^i}{\partial r} \right) - \frac{1}{r^2} \frac{\partial}{\partial \theta} \left(\frac{1}{\sin \theta} \frac{\partial A^i \sin \theta}{\partial \theta} \right) = B^i f^i(t, r) \Phi^i(\theta) \quad (26)$$

where the meaning of $\Phi^i(\theta)$ and B^i is evident from Eq. (21). Index i will be omitted hereafter. The initial condition is $A(0, r, \theta) = 0$ and the boundary condition is $A|_{r \rightarrow \infty} = 0$. Note that $\Phi^i(\theta)$ are not arbitrary functions and they should be invariant to the choice of direction $\theta = 0$ axis. It means $\Phi^i(-\theta) = -\Phi^i(\theta)$, so $\Phi^i = \text{const}$ is not possible due to the physics of our problem. For such a case, the convenient replacement is as follows:

$$A = \sum_{n=1}^{+\infty} a_n p_n w_n \quad (27)$$

where $p_n \equiv P_n^1(\cos \theta)$ are associated Legendre functions which are the solutions of the equation:

$$\frac{\partial}{\partial \theta} \left(\frac{1}{\sin \theta} \frac{\partial p_n \sin \theta}{\partial \theta} \right) + n(n+1) p_n = 0. \quad (28)$$

They consist of an orthonormal basis ($\int_{-1}^1 p_n p_j d \cos \theta = 0$, if $n \neq j$ and $\int_{-1}^1 p_n^2 d \cos \theta = 2n(n+1)/(2n+1)$), so $p_0 = 0$ (Gradshteyn and Rizik, 1963, p. 1012). Hence, the coefficients a_n can be easily determined:

$$a_n = \frac{2n+1}{2n(n+1)} \int_{-1}^1 \Phi(\theta) p_n d(\cos \theta) \quad (29)$$

As a result, w_n is a solution of the following equation:

$$\frac{1}{D} \frac{\partial w_n}{\partial t} - \frac{1}{r^2} \frac{\partial}{\partial r} \left(r^2 \frac{\partial w_n}{\partial r} \right) + \frac{n(n+1)}{r^2} w_n = B f(t, r). \quad (30)$$

It is shown in Molchanov et al. (2001) that the solution can be expressed as follows:

$$w_n(t, r) = B \int_0^t d\tau \int_0^{+\infty} \frac{f(\tau, \rho)}{\sqrt{r}} \frac{1}{2D(t-\tau)} e^{-\frac{r^2+\rho^2}{4D(t-\tau)}} I_{n+1/2} \left(\frac{r\rho}{2D(t-\tau)} \right) \rho^{3/2} d\rho \quad (31)$$

where $I_{n+1/2}(z)$ is the modified Bessel function of the order

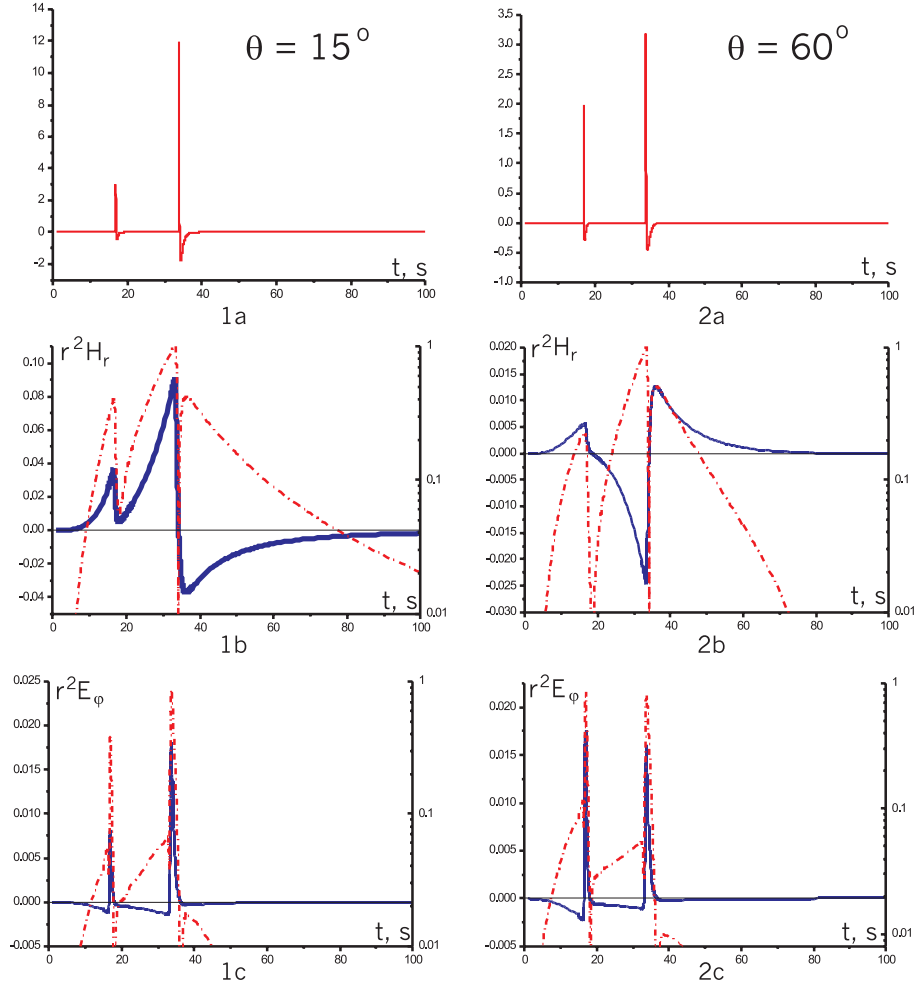


Fig. 5. Seismic source (a), $r^2 H_r$ (b), $r^2 E_\phi$ (c) as a function of t ; $r = 100$ km, $L_s = 3$ km, $\theta = 15^\circ$ (1) or $\theta = 60^\circ$ (2), $C_p = 6$ km/s, $C_s = 3$ km/s, $D = 200$ km²/s. Dash-dot lines show the value of $|H_r|/\max|H_r|$ (2) and $|E_\phi|/\max|E_\phi|$ (3) in logarithmic coordinates.

of $n + 1/2$. Note that in the case of $n = 0$, it reduces to the well-known Poisson solution of the diffusion equation.

$$\begin{aligned}
 w_0(t, r) &= \frac{B}{\pi} \int_0^t \int_{V_p} \frac{1}{(4D(t-\tau))^{3/2}} e^{-\frac{|r-\rho|^2}{4D(t-\tau)}} dV_\rho d\tau \\
 &= \frac{B}{\pi} \int_0^t d\tau \int_0^\pi \sin\theta' d\theta' \int_0^{2\pi} d\varphi' \int_0^{+\infty} \\
 &\quad \frac{1}{(4D(t-\tau))^{3/2}} e^{-\frac{r^2 + \rho^2 - 2r\rho(\cos\theta \cos\theta' + \sin\theta \sin\theta' \cos\varphi')}{4D(t-\tau)}} d\rho \\
 &= \frac{B}{\sqrt{\pi}} \int_0^t \frac{d\tau}{\sqrt{D(t-\tau)}} \int_0^{+\infty} \\
 &\quad f(\tau, \rho) \frac{\rho}{2r} \left(e^{-\frac{(r-\rho)^2}{4D(t-\tau)}} - e^{-\frac{(r+\rho)^2}{4D(t-\tau)}} \right) d\rho. \quad (32)
 \end{aligned}$$

In our case, $n = 1$, and $n = 3$. Then we have

$$w_n(t, r) = \frac{B}{\sqrt{\pi}} \int_0^t \frac{d\tau}{\sqrt{D(t-\tau)}} \int_0^{+\infty} f(\tau, \rho) F_n(D(t-\tau), \rho, r) d\rho, \quad n = 1, 3 \quad (33)$$

where

$$\begin{aligned}
 F_1(a, \rho, r) &= \frac{\rho}{r} Cs(a, \rho, r) - \frac{2a}{r^2} Sn(a, \rho, r), \\
 F_3(a, \rho, r) &= \left(\frac{\rho}{r} + \frac{60a^2}{\rho r^3} \right) Cs(a, \rho, r) \\
 &\quad - \left(\frac{12a}{r^2} + \frac{120a^3}{r^4 \rho^2} \right) Sn(a, \rho, r), \\
 Cs(a, \rho, r) &= \frac{1}{2} \left(e^{-\frac{(r-\rho)^2}{4a}} + e^{-\frac{(r+\rho)^2}{4a}} \right), \\
 Sn(a, \rho, r) &= \frac{1}{2} \left(e^{-\frac{(r-\rho)^2}{4a}} - e^{-\frac{(r+\rho)^2}{4a}} \right).
 \end{aligned}$$

5 Result of computations

We use Eq. (21) for an induced source. Let us calculate the coefficients a_n for the case of a tension crack:

$$\sin\theta(1 + \cos^2\theta) = \frac{6}{5} p_1(\cos\theta) + \frac{2}{15} p_3(\cos\theta),$$

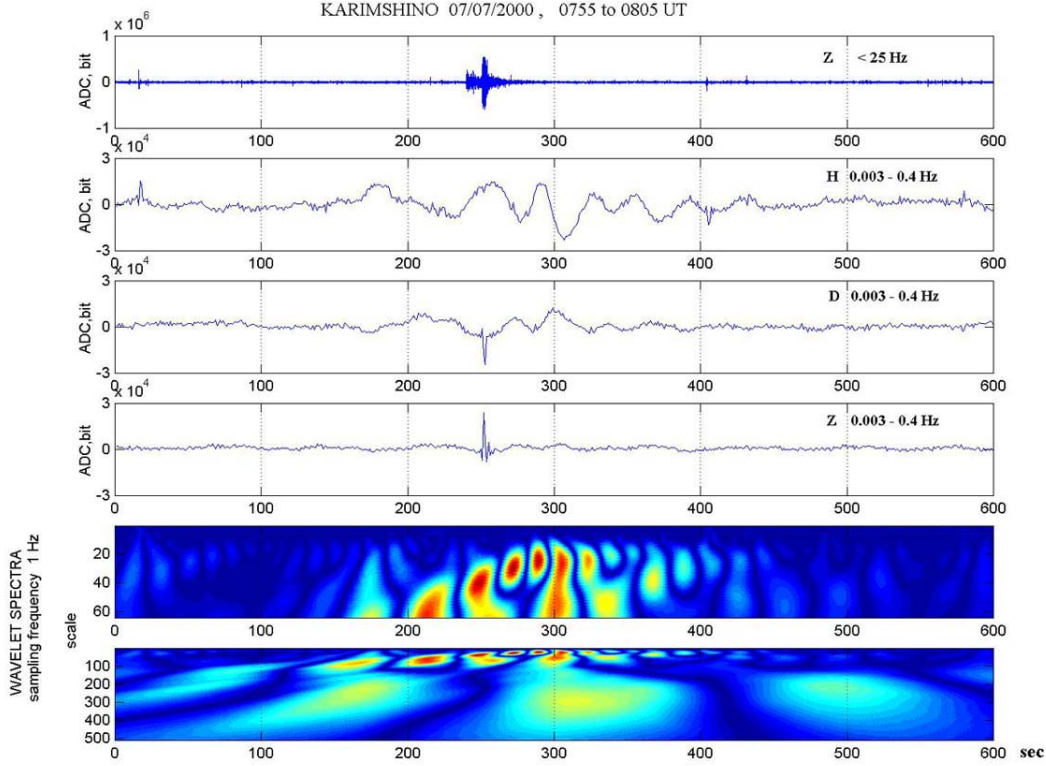


Fig. 6. Seismic pulse (above) together with coseismic variations in the H , D , Z components of the magnetic field (0.003–0.4 Hz frequency range, next panels) and wavelet spectrum of H -variations (below) observed at Karimshino station, Kamchatka, Russia. Hypocentral distance is ≈ 86 km and $M_s = 3.8$ in this case. Influence by shaking in the magnetic field is coincident with the maximal spike inside the seismic train, but the total duration of magnetic pulse τ_m essentially exceeds the length of the seismic pulse τ_s and their ratio $rt = \tau_m/\tau_s \approx 30$.

$$\sin \theta \cos^2 \theta = \frac{1}{5} p_1(\cos \theta) + \frac{2}{15} p_3(\cos \theta). \quad (34)$$

We use Eq. (33) for the calculations when $B = 1$. Some results of the calculation are shown in Fig. 4 and Fig. 5. Fig. 4 shows the plots of $r^2 H_r$ as a function of t for $L_s = 1$ and distances of 50, 100 and 150 km. It is clear that the value of H_r decreases as $\sim 1/r^2$.

Plots of the source (1a, 1b), H_r (2a, 2b) and E_φ (3a, 3b) for $\theta = 15^\circ$, $\theta = 60^\circ$ are shown in Fig. 5. To define an elongation of the magnetic field and electric field, we placed the graphics of $|H_r|/\max |H_r|$ and $|E_\varphi|/\max |E_\varphi|$ in logarithmic coordinates (dash-dot line).

6 Discussion and conclusions

We have tried to demonstrate that consideration of the penetration of a low-frequency wave through a conductive medium is rather simplified if we solve the equations of electromagnetic diffusion by a double-potential method. This approach is related to the specific gauge condition, which was justified in detail here. Of course, the solutions are not so simple when taking into consideration inhomogeneity and

the presence of boundaries at the real medium. But even in this situation, the discussed solutions could be useful for estimates (assuming some averaged parameters) or for computations in the case of an inhomogeneous medium.

The most prominent feature of the seismo-inductive effect is the elongation of magnetic and electric pulses in comparison with the duration of the seismic pulse, as demonstrated in Fig. 5. Nagao et al. (2000) found that duration of coseismic electric pulses are sometimes exceeding essentially the length of the corresponding seismic pulses. They interpreted this in terms of electro-kinetic phenomenon, but a seismo-inductive effect explanation is also possible. Recently, some indication of coseismic magnetic pulses have probably been found in Kamchatka ULF observations (description of the observations is presented in Gladyshev et al., 2001). An example is shown in Fig. 6.

Of course, there is no exact coincidence in theoretical and observational results; however, a tendency of magnetic pulse elongation is evident from both pictures in Fig. 5 and Fig. 6.

It is known that a variety of seismic shocks could happen in a time of foreshock activity during several days before a large earthquake. The usual seismic spectrum has a maximum near $\omega/2\pi \sim \omega_c/2\pi \sim 1$ Hz (see e.g. Molchanov et

al., 2001). Let us imagine what will happen with the magnetic and electric variations, taking into account a possibility of the inductive effect discussed here. We can expect an appearance of specific electromagnetic “noise” whose spectrum maximum is reduced down to $\omega/2\pi \sim 1\text{Hz}/rt \sim 0.01 - 0.05\text{ Hz}$. Such phenomena in the shown frequency range have been observed indeed as ULF electromagnetic emission and they are well discussed just in this monograph. We can expect, furthermore, that this ULF emission (if resulted from an inductive effect) should have the same limitation in the area of observation as foreshock seismic shocks themselves. In the case of EQ with $M_s \sim 5 - 6$, the usual values of foreshock magnitudes which occur near the hypocentral region are about 3–4 ($L_s \sim 1 - 2\text{ km}$) and the attenuation distance for them is $R_a \approx QL_s \sim 100 - 200\text{ km}$. Similar limiting distance in the observation of precursory ULF magnetic emission was often reported. In fact, this limitation is more severe for electromagnetic pulses due to the $\sim 1/r^2$ dependence of their amplitudes even in the region ($r \leq R_a$) without attenuation as evident from Fig. 5 and unlike the geometrical factor $1/r$ for the seismic pulses.

Our modeling is greatly simplified due to the suppositions of an inhomogeneous medium, the special form of the fracture (in reality, shear crack is more probable) and the orientation of the fracture plane to the direction of the external magnetic field. It is interesting to note that some important features of the seismo-inductive effect are revealed even in this oversimplified consideration.

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